

Contents

1 FIGURE 5 – BACCALA ET AL. (2016) DTF: UNIFIED ASYMPTOTIC THEORY	1
Generating data set for analysis	1
Equation 2	2
Connectivity diagram	2
DTF estimation	4
PDC estimation	5
$ PDC(\lambda) ^2$ Matrix Layout Plotting	6
Figure depicted in the article Baccala et al (2016)	6
Some remarks:	7

1 FIGURE 5 – BACCALA ET AL. (2016) DTF: UNIFIED ASYMP-TOTIC THEORY

DESCRIPTION:

Routine `figure5_example2_ipdc_idtf_ns500.m` publish

Linear trivariate VAR(2) model

LA Baccala, DY Takahashi, K Sameshima (2016) Directed Transfer Function: Unified Asymptotic Theory and Some of its Implications. *IEEE Transactions on Biomedical Engineering* **PP**.

<http://dx.doi.org/10.1109/TBME.2016.2550199>

Example 2: Trivariate loop VAR(2) model

```
x1 ==> x2 ==> x3  
^-----/
```

Contents

- Generating data set for analysis
- Equation 2
- Connectivity diagram
- DTF estimation
- PDC estimation
- $|PDC(\lambda)|^2$ Matrix Layout Plotting
- Figure depicted in the article Baccala et al (2016)
- Some remarks:

Generating data set for analysis

```
clear; clc; format compact  
flgPlotStyle = 'Print'; % or 'Screen' mode  
flgRandomize = 0; % Generate the specific data set used in Fig. 1.  
ns = 500; % number of sample points  
nDiscard = 20000; % number of points discarded at beginning of simulation  
p = 2; % model order  
  
if (exist('figure5_example2_ipdc_idtf_ns500.mat') == 2) & is_octave & ~  
    flgRandomize,  
    load figure5_example2_ipdc_idtf_ns500  
else
```

```

[u] = fbaccala2016_example2( ns, nDiscard, flgRandomize );
if ~is_octave & ~flgRandomize,
    save figure5_example2_ipdc_idtf_ns500 u
end;
end;

chLabels = [];% Using default labeling schema for channel identification

```

=====
"DTF Unified Asymptotic Theory" Example 2
x1 ==> x2 ==> x3
^-----/
=====

Equation 2

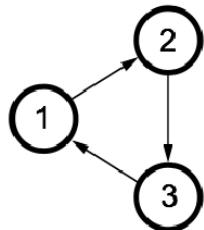
$$\begin{aligned}
x_1(n) &= 0.95\sqrt{2}x_1(n-1) - 0.9025x_1(n-2) \\
&\quad + 0.35x_3(n-1) + w_1(n) \\
x_2(n) &= 0.5x_1(n-1) + 0.5x_2(n-1) + w_2(n) \\
x_3(n) &= x_2(n-1) - 0.5x_3(n-1) + w_3(n)
\end{aligned}$$

Equation (9) from Baccala et al. *IEEE Trans Biomed Engin.*, 2016.

with the innovations covariance matrix given by

$$\Sigma_w = \begin{bmatrix} 1 & 5 & 0.3 \\ 5 & 100 & 2 \\ 0.3 & 2 & 1 \end{bmatrix}$$

Connectivity diagram



Example 2 loop connectivity structure following (9) and (10). Signals from any structure reach all other structures. from Baccala et al. *IEEE Trans Biomed Engin.*, 2016.

Data pre-processing: detrending and normalization options

```

flgDetrend = 1;      % Detrending the data set
flgStandardize = 0; % No standardization
[nChannels,nSegLength] = size(u);
if nChannels > nSegLength, u = u.';
[nChannels,nSegLength] = size(u);
end;
if flgDetrend,
for i=1:nChannels, u(i,:) = detrend(u(i,:)); end;
disp('Time series were detrended.');
end;
if flgStandardize,
for i=1:nChannels, u(i,:) = u(i,:)/std(u(i,:)); end;
disp('Time series were scale-standardized.');
end;

```

Time series were detrended.

MVAR model estimation

```

maxIP = 30;          % maximum model order to consider.
alg = 1;             % 1: Nutall-Strand MVAR estimation algorithm
criterion = 1;        % 1: AIC, Akaike Information Criteria
disp('Running MVAR estimation and GCT analysis routines.')
[IP,PF,A,pb,B,ef,eb,Vaic,Vaicv] = mvar(u,maxIP,alg,criterion);
disp(['Number of channels = ' int2str(nChannels) ' with ' ...
int2str(nSegLength) ' data points; MAR model order = ' int2str(IP) '.']);

```

Running MVAR estimation and GCT analysis routines.

```

maxOrder limited to 30
IP=1  vaic=13036.798425
IP=2  vaic=11418.716167
IP=3  vaic=11427.055278

```

Number of channels = 3 with 500 data points; MAR model order = 2.

Testing for adequacy of MAR model fitting through Portmanteau test

```

h = 20; % testing lag
MVARadequacy_signif = 0.05; % VAR model estimation adequacy significance
                             % level
aValueMVAR = 1 - MVARadequacy_signif; % Confidence value for the testing
flgPrintResults = 1;

```

Granger causality test (GCT) and instantaneous GCT

```

gct_signif = 0.01; % Granger causality test significance level
igct_signif = 0.01; % Instantaneous GCT significance level
flgPrintResults = 1;
[Tr_gct, pValue_gct, Tr_igct, pValue_igct] = gct_alg(u,A,PF,gct_signif, ...
igct_signif,flgPrintResults);

```

GRANGER CAUSALITY TEST
=====

Connectivity matrix:

NaN	0	1
-----	---	---

```

      1     NaN      0
      0     1     NaN
Granger causality test p-values:
      NaN      0.1256      0
      0.0000      NaN      0.1175
      0.4488      0      NaN
-----
                           INSTANTANEOUS GRANGER CAUSALITY TEST
=====
Instantaneous connectivity matrix:
      NaN      1      1
      1     NaN      1
      1      1     NaN
Instantaneous Granger causality test p-values:
      1.0e-06 *
      NaN      0      0.0000
      0      NaN      0.5589
      0.0000      0.5589      NaN
>>> There are 3 pairs of channels with
      significant Instantaneous Causality.

```

DTF estimation

DTF analysis results are saved in **c** structure. See `asymp_dtf.m` or issue `>> help asymp_dtf` command for more detail.

```

metric = 'info'; % euc = original PDC or DTF;
                  % diag = generalized PDC (gPDC) or directed coherence (DC);
                  % info = information PDC (iPDC) or iDTF.

nFreqs = 128;
alpha = 0.01;

c = asymp_dtf(u,A,PF,nFreqs,metric,alpha);

* Information DTF and asymptotic statistics

```

$|DTF(\lambda)|^2$ Matrix Layout Plotting

```

switch lower(flgPlotStyle)
  case 'print'
    flgColor =[0]; % white background
    flgMax = 'TCI';
    flgSignifColor = 1; % black + gray
    flgScale = 2; % [0 max(flgMax)]
  otherwise % 'screen'
    flgColor =[1]; % Colored background
    flgMax = 'TCI';
    flgSignifColor = 3; % red + green
    flgScale = 2; % [0 1]/[0 .1]/[0 .01]
end;

% -----Plotting options flag setting-----
%          [1 2 3 4 5 6 7]
flgPrinting=[1 1 1 2 2 0 0];
%          | | | | | 7 Spectra(0: w/o SS; 1: Linear; 2: log-scale)

```

```

%
% | | | | 6 Coherence
% | | | | 5 Plot lower confidence limit (legacy)
% | | | | 4 Plot upper confidence limit
% | | | 3 Significant DTF(w) in red line (legacy)
% | | 2 Patnaik threshold level in black dashed-line
% | 1 plot DTF
%-----

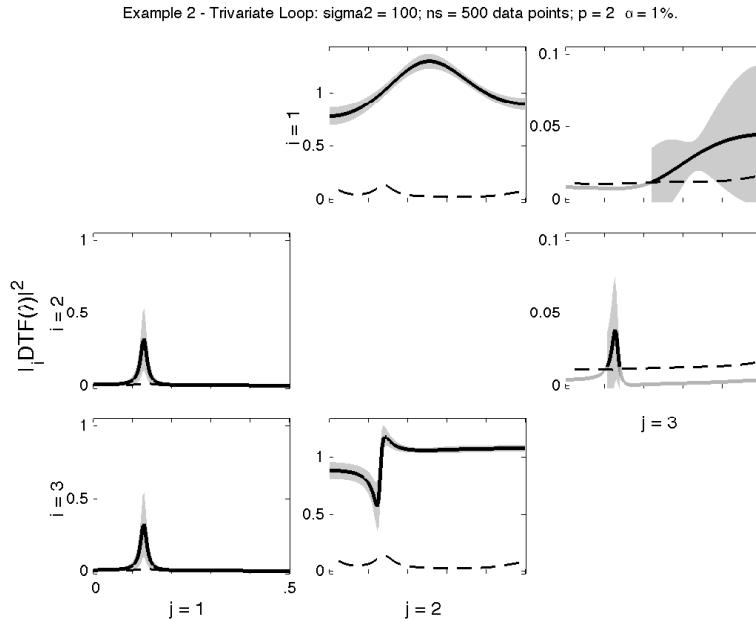
fs = 1; % sampling frequency

w = fs*(0:(nFreqs-1))/2/nFreqs;
w_max = fs/2;

h = figure;
set(h, 'NumberTitle','off', 'MenuBar', 'none', ...
    'Name', '[Asymptotic DTF] Fig 5. Example 2 - Trivariate loop iDTF, ns = 500')
[h xlabel ylabel] = xplot(c, ...
    flgPrinting, fs, w_max, chLabels, flgColor, flgScale, flgMax, flgSignifColor);
%xplot_title(alpha, metric, measure(c));

[ax, hT] = suplabel(['Example 2 - Trivariate Loop: sigma2 = 100; ns = ' ...
    int2str(ns) ' data points; p = ' int2str(p) ' \alpha = ' ...
    int2str(100*alpha) '%.' ], 't');
set(hT, 'FontSize', 10); % Subtitle font size

```



Uncomment the command line bellow to generate an eps output file

```
% print -depsc2 -painters Fig5_example2_dtf_ns500.eps
```

PDC estimation

PDC analysis results are saved in **d** structure. See `asymp_dtf.m` or issue `>> help asymp_pdc` command for more detail.

```

nFreqs = 128;
metric = 'info'; % euc = Euclidian = original PDC;
% % diag = diagonal = generalized PDC or gPDC;
% % info = information = iPDC
alpha = 0.01;

d = asymp_pdc(u,A,pf,nFreqs,metric,alpha);

% Power spectra and coherence calculation
d.SS = ss_alg(A, pf, nFreqs);
d.coh = coh_alg(d.SS);

if alpha ~= 0,
    % Statistically significant PDC on frequency scale
    pdc_temp = ((abs(d.pdc)-d.th) > 0).*d.pdc + ((abs(d.pdc)-d.th) <= 0)*(-1);
    pdc_temp(ind2sub(size(pdc_temp),find(pdc_temp == -1))) = NaN;
    d.pdc_th = pdc_temp;
end;

* Information PDC and asymptotic statistics

```

$|PDC(\lambda)|^2$ Matrix Layout Plotting

```

% -----Plotting options flag setting-----
% [1 2 3 4 5 6 7]
flgPrinting=[1 1 1 2 2 0 0];
% | | | | | 7 Spectra(0: w/o SS; 1: Linear; 2: log-scale)
% | | | | 6 Coherence
% | | | | 5 Plot lower confidence limit (legacy)
% | | | | 4 Plot upper confidence limit
% | | | 3 Significant DTF(w) in red line (legacy)
% | | 2 Patnaik threshold level in black dashed-line
% 1 plot DTF
%-----
fs = 1; % sampling frequency
w_max = fs/2; % x-axis maximum value
h = figure;
set(h,'NumberTitle','off','MenuBar','none',...
    'Name','[Asymptotic DTF] Fig5. Example 2 - Trivariate loop ipDC, ns = 500')
[h xlabel ylabel] = xplot(d,...
    flgPrinting,fs,w_max,chLabels,flgColor,flgScale,flgMax,flgSignifColor);

%xplot_title(alpha,metric, measure(c));

[ax,hT]=suplabel(['Example 2 - Trivariate Loop: sigma2 = 100; ns = ' ...
    int2str(ns) ' data points; p = ' int2str(p) ' \alpha = ' ...
    int2str(100*alpha) '%.' ],'t');
set(hT,'FontSize',10); % Subtitle font size

```

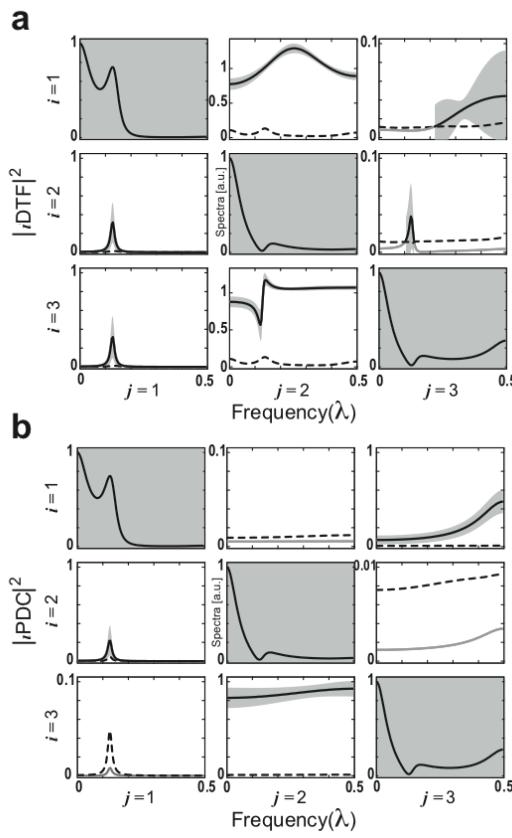
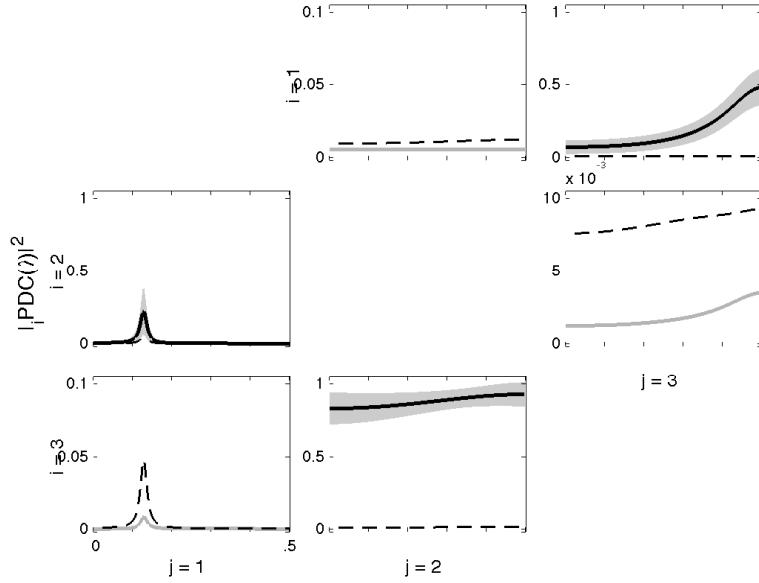
Uncomment the command line bellow to generate an eps output file

```
print -depsc2 -painters Fig5_example2_ipdc_ns500.eps
```

Figure depicted in the article Baccala et al (2016)

Figure 5, reproduced from article.

Example 2 - Trivariate Loop: sigma2 = 100; ns = 500 data points; p = 2 α = 1%.



Some remarks:

1. As usual, figure 5 underwent some cosmetic manipulation.

This completes the Figure 5 generation (Baccala et al, 2016)'